Performance Analysis and Resource Optimisation of Critical Systems Modelled by Petri Nets

Ricardo J. Rodríguez

## Ph.D. DISSERTATION

Advisors: Dr. Jorge Emilio Júlvez Bueno and Dr. José Javier Merseguer Hernáiz



Dpto. de Informática e Ingeniería de Sistemas, Universidad de Zaragoza

June 24th, 2013

Zaragoza, Spain

#### Outline



## Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling
- Operation Performance Analysis
  - Some Background...
  - Regrowing Strategy for SMGs
  - Regrowing Strategy for PPNs

#### 4 Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results



#### Resource Optimisation

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
- Problem Description
- Performance Analysis
- Resource Optimisation
- Conclusions



#### Security and FTTs Modellin

- Security Modelling
- Fault-Tolerant Techniques Modelling
- Performance Analysis
  - Some Background. . .
  - Regrowing Strategy for SMGs
  - Regrowing Strategy for PPNs

#### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

#### **Resource Optimisation**

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
- Problem Description
- Performance Analysis
- Resource Optimisation
- Conclusions

## Vulnerable Critical Systems

- Mission must be accomplished in hostile environments
  - Vulnerable
  - Internal or external faults
- E.g. SCADA systems, avionics, aerospace, manufacturing, logistics...



## Vulnerable Critical Systems

- Mission must be accomplished in hostile environments
  - Vulnerable
  - Internal or external faults
- E.g. SCADA systems, avionics, aerospace, manufacturing, logistics...



## Vulnerable Critical Systems

- Mission must be accomplished in hostile environments
  - Vulnerable
  - Internal or external faults
- E.g. SCADA systems, avionics, aerospace, manufacturing, logistics...



## Vulnerable Critical Systems

- Mission must be accomplished in hostile environments
  - Vulnerable
  - Internal or external faults
- E.g. SCADA systems, avionics, aerospace, manufacturing, logistics...



#### Fault-Tolerant Systems

- Critical systems that add FT mechanisms to deal with faults
  - E.g., watchdog, rollback, rollforward, etc.
- Shared resources, naturally modelled as Resource Allocation System (RAS)  $\rightarrow$  resources can be compromised or fail
- Modelled by UML as semi-formal model language
- Petri nets (PNs) as formal model language

R.J. Rodríguez

Ph.D. Dissertation

## Motivation (II): What else?

## Expressing Requirements when Designing a System...

• Requirement: a property of the system

## Motivation (II): What else?

### Expressing Requirements when Designing a System...

#### • Requirement: a property of the system

- Functional: how the system is supposed to behave
  - Technical data, data processing. . .
- Non-functional (NFP): how the system is supposed to perform
  - Usability, performance, reliability...
  - E.g: how many customers can be attended by a web service? how many bytes can be transferred? how many bytes can be ciphered?

## Motivation (III): Where does security fit in?

#### Security: the Forgotten One

- Non-functional property of the system
- Lack of interest
- Consequence: "fix it later"
  - Fix the problem when the problem arises...

## Motivation (III): Where does security fit in?

### Security: the Forgotten One

- Non-functional property of the system
- Lack of interest
- Consequence: "fix it later"
  - Fix the problem when the problem arises...
- Severe consequences
  - High cost reimplementation/redesign
  - Economic losses
  - $\bullet \ \ \mathsf{Down \ services} \to \mathsf{less \ customers}$
  - Disclosure of confidential data (e.g., Sony PSN, RSA company)

## Motivation (III): Where does security fit in?

### Security: the Forgotten One

- Non-functional property of the system
- Lack of interest
- Consequence: "fix it later"
  - Fix the problem when the problem arises...
- Severe consequences
  - High cost reimplementation/redesign
  - Economic losses
  - $\bullet \ \ \mathsf{Down \ services} \to \mathsf{less \ customers}$
  - Disclosure of confidential data (e.g., Sony PSN, RSA company)

# Security: from the beginning to the end

## Motivation (IV): Considering Security in Early Stages Main Contributions of this Dissertation

## SecAM: A UML Profile for Security Analysis and Modelling

- UML tailored for specific purposes: profiling
- Cryptography, Access Control, Security Mechanisms, ...
- Enables quantitative analysis

## Motivation (IV): Considering Security in Early Stages Main Contributions of this Dissertation

## SecAM: A UML Profile for Security Analysis and Modelling

- UML tailored for specific purposes: profiling
- Cryptography, Access Control, Security Mechanisms, ...
- Enables quantitative analysis

#### Fault-Tolerant Techniques models

- Using UML and Petri nets (PNs)
- Composable models
- Allows to introduce different security models
  - Find appropriate security strategies while meeting performance requirements
- From UML to PNs to analyse

## Motivation (V): Just add security, fine...anything else?

• Security addition to a system is not free

## Motivation (V): Just add security, fine...anything else?

- Security addition to a system is not free
- Can affect other NFPs
  - E.g. the more security, the lower system performance
- Other trade-offs exist: availability, usability, economic
- Our main interest: performance
  - Throughput: jobs completed per unit of time

## Motivation (V): Just add security, fine...anything else?

- Security addition to a system is not free
- Can affect other NFPs
  - E.g. the more security, the lower system performance
- Other trade-offs exist: availability, usability, economic
- Our main interest: performance
  - Throughput: jobs completed per unit of time

#### Contribution: A Model-based Methodology

- Quantitative estimation of performance-security trade-off
- Fault-Tolerant Techniques (FTTs) + Security Mechanisms (SMs)
  - FTTs: watchdog, switch over failing, proactive-reactive recovery, ...
  - SMs: (de)encryption, digital signature generation and verification, ...
- Goal: To compose security models with software architectural models

## Motivation (VI): The BUT...(1)

## • Recall: FT systems modelled with Petri nets (PNs)

- More precisely, process Petri nets (PPNs)
  - Good modelling capabilities
  - Interesting analysis skills...

# Motivation (VI): The BUT...(1)

## • Recall: FT systems modelled with Petri nets (PNs)

- More precisely, process Petri nets (PPNs)
  - Good modelling capabilities
  - Interesting analysis skills. . .
- State explosion problem: sooooo large
  - Computation of performance becomes unachievable

# Motivation (VI): The BUT...(1)

- Recall: FT systems modelled with Petri nets (PNs)
  - More precisely, process Petri nets (PPNs)
    - Good modelling capabilities
    - Interesting analysis skills. . .
- State explosion problem: sooooo large
  - Computation of performance becomes unachievable
- Avoid exact computation: upper throughput bounds
  - Using Linear Programming (LP) techniques
  - Good accuracy computational complexity trade-off

# Motivation (VI): The BUT...(2)

#### Contribution: Strategies for Upper Thr. Bounds Computation

- Iterative strategies: The *regrowing* approach
- Close to the real throughput
- For Stochastic Marked Graphs and Stochastic Process Petri nets
- Implemented in a tool: PeabraiN

# Motivation (VI): The BUT...(2)

#### Contribution: Strategies for Upper Thr. Bounds Computation

- Iterative strategies: The regrowing approach
- Close to the real throughput
- For Stochastic Marked Graphs and Stochastic Process Petri nets
- Implemented in a tool: PeabraiN

## Contribution: Data-throttling in Scientific Workflows

- Minimise use of input buffers at tasks
- Better use of network bandwidth
- Also a quantitative metric for evaluating optimisation
- Implemented in a tool: DT4SW (not yet released)

# Motivation (VI): The BUT...(3)

- Recall: security addition is not free
  - Performance, availability, etc. can be influenced

## Motivation (VI): The BUT...(3)

- Recall: security addition is not free
  - Performance, availability, etc. can be influenced
- FT systems with shared resources
  - Can we add more resources to compensate throughput degradation?

## Motivation (VI): The BUT...(3)

- Recall: security addition is not free
  - Performance, availability, etc. can be influenced
- FT systems with shared resources
  - Can we add more resources to compensate throughput degradation?
- $\bullet~$  It depends  $\rightarrow$  resource addition IS NOT free either
  - But let us try something...

## Motivation (VI): The BUT...(3)

- Recall: security addition is not free
  - Performance, availability, etc. can be influenced
- FT systems with shared resources
  - Can we add more resources to compensate throughput degradation?
- $\bullet~$  It depends  $\rightarrow$  resource addition IS NOT free either
  - But let us try something...

## Contribution: Compensation of Throughput Degradation

- Several algorithms to compensate throughput degradation
- Subject to a (major) constraint: Budget

## Motivation (VI): The BUT...(3)

- Recall: security addition is not free
  - Performance, availability, etc. can be influenced
- FT systems with shared resources
  - Can we add more resources to compensate throughput degradation?
- It depends  $\rightarrow$  resource addition IS NOT free either
  - But let us try something...

#### Contribution: Compensation of Throughput Degradation

- Several algorithms to compensate throughput degradation
- Subject to a (major) constraint: Budget
  - A LP problem: Maximise throughput via incrementing resources
  - An Integer-LP problem: Minimise cost of compensating, considering either:
    - Number of resources
    - Timing of FT techniques added



#### Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling
- Performance Analysis
- Some Background. . .
- Regrowing Strategy for SMGs
- Regrowing Strategy for PPNs

#### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

(

#### Resource Optimisation

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
  - Problem Description
  - Performance Analysis
  - Resource Optimisation
- Conclusions

#### UML profile: what?

- OMG standard
- Stereotypes and tagged values to annotate UML elements

#### UML profile: what?

- OMG standard
- Stereotypes and tagged values to annotate UML elements
  - Expressing Non-Functional Properties (NFP) on the UML designs
  - Extending model semantics

## UML profile: what?

- OMG standard
- Stereotypes and tagged values to annotate UML elements
  - Expressing Non-Functional Properties (NFP) on the UML designs
  - Extending model semantics

#### Some examples

- Modelling and Analysis of RT Embedded systems (MARTE)
  - Support for performance and schedulability analysis
  - NFPs expressed thru VSL (Value Specification Language) syntax

## UML profile: what?

- OMG standard
- Stereotypes and tagged values to annotate UML elements
  - Expressing Non-Functional Properties (NFP) on the UML designs
  - Extending model semantics

#### Some examples

- Modelling and Analysis of RT Embedded systems (MARTE)
  - Support for performance and schedulability analysis
  - NFPs expressed thru VSL (Value Specification Language) syntax
- Dependability Analysis and Modelling (DAM)
  - MARTE specialisation
  - Dependability properties into UML

OMG. A UML profile for Modeling and Analysis of Real Time Embedded Systems (MARTE). Document ptc/09-11-02, 2009

Bernardi, S. et al. Model-driven Dependability Assessment of Software Systems. Springer, 2013

# Security Modelling (II): What is security indeed?

Tight relation with *dependability* (Avizienis)



Avizienis, A. et al. Basic Concepts and Taxonomy of Dependable and Secure Computing. IEEE Trans. Dep. Sec. Comp., 2004

## Security Modelling (III): The SecAM profile (1)

Security Analysis and Modelling: A general overview...



## Security Modelling (III): The SecAM profile (2) Cryptography package



## Security Modelling (III): The SecAM profile (3) SecurityMechanisms package


# Security Modelling (III): The SecAM profile (3) *Resilience* package



#### Security Modelling (III): The SecAM profile (4) AccessControl package



## Security Modelling (IV): A Case Study (1)

Problem description

#### Problem

- Services on-demand system
- 2 kind of services
  - Service 1: 1s
  - Service 2: 2s
- Maximum of simultaneous requests: 100



## Security Modelling (IV): A Case Study (1)

Problem description

#### Problem

- Services on-demand system
- 2 kind of services
  - Service 1: 1s
  - Service 2: 2s
- Maximum of simultaneous requests: 100
- Legitimate and illegitimate users



#### Security Modelling (IV): A Case Study (1) Problem description

#### Problem

- Services on-demand system
- 2 kind of services
  - Service 1: 1s
  - Service 2: 2s
- Maximum of simultaneous requests: 100
- Legitimate and illegitimate users



## Security Modelling (IV): A Case Study (2)

Using SecAM: Season to taste the UML model



- 2 possibilities:
  - IDPS1 (hit rate 80%)
  - IDPS2 (hit rate 95%)

#### Security Modelling (IV): A Case Study (3) More models...



#### Security Modelling (IV): A Case Study (3) More models...



# Security Modelling (IV): A Case Study (4) Experiments and results

#### Experiments parameters

- Input customers ratio: {5, 10, 20} customers/s
- IDPS hit rate: 80%, 95%
- Attacks rate: [0.15%...37.5%]

# Security Modelling (IV): A Case Study (4) Experiments and results

#### Experiments parameters

- Input customers ratio:  $\{5, 10, 20\}$  customers/s
- IDPS hit rate: 80%, 95%
- Attacks rate: [0.15%...37.5%]



#### Figure: Hit rate 80%

Figure: Hit rate 95%

#### FTTs Modelling (I): Some Background...



Phases in a FT actuation

Aims at fault avoidance carrying out error detection and system recovery

R.J. Rodríguez

Avizienis, A. et al. Basic Concepts and Taxonomy of Dependable and Secure Computing. IEEE Trans. Dep. Sec. Comp., 2004

#### FTTs Modelling (II): Based on PNs (1)

# Integration with a system Fault-Tolerant model Error Detection model Model System model Operation Petri net Aggregation Interaction through places and/or transitions of Petri nets

#### FTTs Modelling (II): Based on PNs (1)



#### Transformation Rule

- Transition that fails: T<sub>f</sub>
- Adding pre and post places  $\rightarrow$  allows model composition

#### FTTs Modelling (II): Based on PNs (2) Error Detection model



#### FTTs Modelling (II): Based on PNs (3) Recovery model



R.J. Rodríguez

#### FTTs Modelling (II): Based on PNs (4) Running Example (1): a packet-routing algorithm



### FTTs Modelling (II): Based on PNs (4) Running Example (2): a packet-routing algorithm with FT capabilities – reconfiguration with rollbackward



#### FTTs Modelling (III): Based on UML (1)

#### Fault-Tolerant Techniques (FTTs) model library

- Contains a set of FTTs modelling through UML
- Annotated with MARTE-DAM-SecAM profiles

#### FTTs Modelling (III): Based on UML (1)

#### Fault-Tolerant Techniques (FTTs) model library

- Contains a set of FTTs modelling through UML
- Annotated with MARTE-DAM-SecAM profiles
- Composable models
- Allows to introduce different security models
  - Find appropriate security strategies while meeting performance requirements

#### FTTs Modelling (III): Based on UML (1)

#### Fault-Tolerant Techniques (FTTs) model library

- Contains a set of FTTs modelling through UML
- Annotated with MARTE-DAM-SecAM profiles
- Composable models
- Allows to introduce different security models
  - Find appropriate security strategies while meeting performance requirements
- Converted to PNs and analysed

#### FTTs Modelling (III): Based on UML (2) A Proactive-Reactive Recovery Technique (1)



Security and FTTs Modelling Fault-T

Fault-Tolerant Techniques Modelling

#### FTTs Modelling (III): Based on UML (2) A Proactive-Reactive Recovery Technique (2)



Security and FTTs Modelling Fault-

Fault-Tolerant Techniques Modelling

#### FTTs Modelling (III): Based on UML (2) A Proactive-Reactive Recovery Technique (2)



«gaAnalysisContext»

{contextParams=in\$nDevices,in\$detect,in\$rRecovery,in\$pRecovery}



#### FTTs Modelling (III): Based on UML (3) Switch Over Failing



R.J. Rodríguez

Security and FTTs Modelling Fault-Tolerant

Fault-Tolerant Techniques Modelling

#### FTTs Modelling (III): Based on UML (4) Ping and Restore



R.J. Rodríguez

#### Motivation

3

#### Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling

#### Performance Analysis

- Some Background...
- Regrowing Strategy for SMGs
- Regrowing Strategy for PPNs

#### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

#### **Resource Optimisation**

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
  - Problem Description
  - Performance Analysis
  - Resource Optimisation
- Conclusions

#### Performance Analysis (I): Some background...(1)

#### Petri nets subclasses

- State Machine:  $\forall t \in T, |t^{\bullet}| = |^{\bullet}t| = 1$
- Marked Graph:  $\forall p \in P, |\bullet p| = |p^{\bullet}| = 1$

#### Performance Analysis (I): Some background...(1)

#### Petri nets subclasses

- State Machine:  $\forall t \in T, |t^{\bullet}| = |^{\bullet}t| = 1$
- Marked Graph:  $\forall p \in P, |\bullet p| = |p^{\bullet}| = 1$

#### Process Petri nets (PPNs): a (really) interesting subclass

- Shared resources systems
- Any process which involves resource usage to complete
- Different jobs with dissimilar handling
- Examples: Assembly lines, Service-Oriented-Architecture systems...

Ph.D. Dissertation, Universidad de Zaragoza, 2003

Tricas F., Deadlock Analysis, Prevention and Avoidance in Sequential Resource Allocation Systems.

#### Performance Analysis (I): Some background...(2) Informal definition of a PPN – an example



#### Performance Analysis (I): Some background...(2) Informal definition of a PPN – an example



• Places can be divided in three subsets:  $P = P_0 \cup P_S \cup P_R$ 

- Process-idle place,  $P_0 = \{p_0\}$
- Process-activity places,  $P_S \neq \emptyset, P_S \cap P_0 = \emptyset, P_S \cap P_R = \emptyset$
- Resources places,  $P_R = \{r_1, \ldots, r_n\}, n > 0, P_R \cap P_0 = \emptyset$

#### Performance Analysis (I): Some background...(2) Informal definition of a PPN – an example



• When removing *P<sub>R</sub>* places, we get a strongly connected state machine, s.t. every cycle contains *p*<sub>0</sub>

R.J. Rodríguez

Ph.D. Dissertation

#### Performance Analysis (I): Some background...(2) Informal definition of a PPN – an example



For each r ∈ P<sub>R</sub>, there exists a unique minimal p-semiflow associated to r, y<sub>r</sub> ∈ N<sup>|P|</sup> s.t. it contains on its support just the resource r and does not contains p<sub>0</sub>

#### Performance Analysis (I): Some background...(2) Informal definition of a PPN – an example



For each r ∈ P<sub>R</sub>, there exists a unique minimal p-semiflow associated to r, y<sub>r</sub> ∈ N<sup>|P|</sup> s.t. it contains on its support just the resource r and does not contains p<sub>0</sub>

#### Performance Analysis (I): Some background...(2) Informal definition of a PPN – an example



 Activity places set P<sub>S</sub> does not contain neither resource places, nor process-idle place

R.J. Rodríguez

Ph.D. Dissertation

June 24th, 2013 37 / 69

## Performance Analysis (I): Some background...(3)

A LPP for a lower bound for the average inter-firing time of transition  $t_i$ 

• Little's law:  $L = \lambda \cdot W$  (queue length, arrival rate, waiting time)

#### Performance Analysis (I): Some background...(3) <u>A LPP for a lower bound for the average inter-firing time of transition $t_i$ </u>

Little's law: L = λ ⋅ W (queue length, arrival rate, waiting time)
m ≥ Pre ⋅ D ⋅ Θ
### Performance Analysis (I): Some background...(3) A LPP for a lower bound for the *average inter-firing time* of transition $t_i$

Little's law: L = λ ⋅ W (queue length, arrival rate, waiting time)
m ≥ Pre ⋅ D ⋅ Θ

 $\begin{aligned} &\textit{Maximize } \Theta: \\ & \overline{\mathbf{m}} \geq \mathbf{Pre} \cdot \mathbf{D} \cdot \Theta \\ & \overline{\mathbf{m}} = \mathbf{m_0} + \mathbf{C} \cdot \sigma \\ & \sigma \geq 0 \end{aligned}$ 

Performance Analysis (I): Some background...(3) A LPP for a lower bound for the *average inter-firing time* of transition  $t_i$ 

Little's law: L = λ · W (queue length, arrival rate, waiting time)
m ≥ Pre · D · Θ



y is the slowest p-semiflow of the system (bottleneck)Our aim: Find next constraining p-semiflow

Campos, J. & Silva, M., Structural Techniques and Performance Bounds of Stochastic Petri Net Models. Advances in PNs, 1992

# Performance Analysis (II): SMGs Regrowing Strategy (1)

Algorithm 1 in the Dissertation

- Input data: SMG, accuracy
- Output data: sharp performance bound, bottleneck

# Performance Analysis (II): SMGs Regrowing Strategy (1)

Algorithm 1 in the Dissertation

- Input data: SMG, accuracy
- Output data: sharp performance bound, bottleneck

### Algorithm steps

- Calculate initial upper throughput bound and initial bottleneck cycle
- Ocalculate tight marking and slacks
  - Computed by a LPP (Carmona et al., Scheduling Synchronous Elastic Designs. ACSD, 2009)
  - The lower the slack, the higher the probability that place will constrain
- Iterate until no significant improvement is achieved
  - Look for place with minimum slack and add it
  - ② Calculate new throughput bound

# Performance Analysis (II): SMGs Regrowing Strategy (2)



# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Θ

%last

-

%initial

# Performance Analysis (II): SMGs Regrowing Strategy (2)



$\sim$				0 01
Con	sider	an	$\epsilon =$	0.01

Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	<i>P</i> 1, <i>P</i> 14	-	0.3704	-	-

# Performance Analysis (II): SMGs Regrowing Strategy (2)



	Consider	an	$\epsilon =$	0.01
--	----------	----	--------------	------

Iteration step	Candidates places	Added	Φ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>P</i> 1	0.3704	-	-

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	-	-	0.322581	12.9%	12.9%

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	<i>P</i> 10, <i>P</i> 14	-	0.322581	12.9%	12.9%

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	<i>p</i> <sub>10</sub> , <i>p</i> <sub>14</sub>	<i>P</i> 10	0.322581	12.9%	12.9%

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	P10, P14	<i>p</i> <sub>10</sub>	0.322581	12.9%	12.9%
2	-	-	0.297914	7.647%	19.563%

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	%initial
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	P10, P14	<i>p</i> <sub>10</sub>	0.322581	12.9%	12.9%
2	<i>P</i> 5, <i>P</i> 11,	-	0.297914	7.647%	19.563%
	<i>P</i> 14, <i>P</i> 15				

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	%initial
	r		r	r	r
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	P10, P14	<i>p</i> <sub>10</sub>	0.322581	12.9%	12.9%
2	$p_5, p_{11},$	<i>P</i> 5	0.297914	7.647%	19.563%
	P14, P15				

# Performance Analysis (II): SMGs Regrowing Strategy (2)



Cor	nside	er an	$\epsilon =$	0.01
		•		

Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	%initial
0	<i>p</i> <sub>1</sub> , <i>p</i> <sub>14</sub>	<i>p</i> 1	0.3704	-	-
1	<i>p</i> <sub>10</sub> , <i>p</i> <sub>14</sub>	<i>p</i> <sub>10</sub>	0.322581	12.91%	12.91%
2	<i>P</i> 5, <i>P</i> 11 <i>P</i> 14, <i>P</i> 15	<i>p</i> 5	0.297914	7.647%	19.563%
3	-	-	0.288401	3.193%	22.137%

# Performance Analysis (II): SMGs Regrowing Strategy (2)



Consid	ler	an	$\epsilon =$	0.01	
					ĉ

00110100					
Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> 1	0.3704	-	-
1	$p_{10}, p_{14}$	P <sub>10</sub>	0.322581	12.9%	12.9%
2	P5, P11, P14, P15	<i>P</i> 5	0.297914	7.647%	19.563%
3	<i>P</i> <sub>11</sub> , <i>P</i> <sub>14</sub> , <i>P</i> <sub>15</sub>	-	0.288401	3.193%	22.137%

# Performance Analysis (II): SMGs Regrowing Strategy (2)



Consider an  $\epsilon = 0.01$ 

Iteration step	Candidates places	Added	Θ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	$p_{10}, p_{14}$	P <sub>10</sub>	0.322581	12.9%	12.9%
2	<i>P</i> 5, <i>P</i> 11, <i>P</i> 14, <i>P</i> 15	<i>p</i> 5	0.297914	7.647%	19.563%
3	P <sub>11</sub> , P <sub>14</sub> , P <sub>15</sub>	P <sub>11</sub>	0.288401	3.193%	22.137%

# Performance Analysis (II): SMGs Regrowing Strategy (2)

A running example for easy understanding



00110100		0.01			
Iteration step	Candidates places	Added	Φ	% <sub>last</sub>	% <sub>initial</sub>
0	$p_1, p_{14}$	<i>p</i> <sub>1</sub>	0.3704	-	-
1	$p_{10}, p_{14}$	<i>p</i> <sub>10</sub>	0.322581	12.9%	12.9%
2	$p_5, p_{11}, p_{14}, p_{15}$	<i>p</i> 5	0.297914	7.647%	19.563%
3	P <sub>11</sub> , P <sub>14</sub> , P <sub>15</sub>	P <sub>11</sub>	0.288401	3.193%	22.137%
4	-	-	0.288401	0%	22.137%

### Performance Analysis (II): SMGs Regrowing Strategy (3) Experiments and Discussion (1)

#### Benchmarking and used tools

- ISCAS benchmark
  - Strongly connected components of the ISCAS graphs
  - Initial marking randomly selected in [1...10]
  - Delay of transitions randomly selected in [0.1...1]
- Strategy implemented in MATLAB (linprog)
- Simulation tool: GreatSPN
  - Confidence level 99%; accuracy 1%
- Host: Pentium IV 3.6GHz, 2GB DDR2 533MHz RAM

### Performance Analysis (II): SMGs Regrowing Strategy (3) Experiments and Discussion (2)

Cranh	Si	ze	%	Size	Regrowing	Initial	Α
Graph	P		P'  (%)	T'  (%)	steps	thr. bound	0
s1423	1107	792	79 (7.13%)	76 (9.59%)	3	0.236010	0.235213 (0.34%)
s1488	1567	1128	91 (5.8%)	86 (7.62%)	6	0.201300	0.173127 (13.99%)
s208	27	24	27 (100%)	24 (100%)	3	0.409390	0.377683 (7.75%)
s27	54	44	19 (35.18%)	18 (40.9%)	1	0.305960	0.304987 (0.31%)
s349	187	146	26 (13.9%)	24 (16.44%)	2	0.340320	0.327867 (3.66%)
s444	92	68	14 (15.21%)	12 (17.64%)	2	0.181670	0.181260 (0.22%)
s510	1038	734	45 (4.33%)	40 (5.45%)	5	0.133030	0.117819 (11.43%)
s526	113	92	18 (15.93%)	16 (17.39%)	2	0.313490	0.305860 (2.43%)
s713	271	208	11 (4.06%)	10 (4.8%)	1	0.428720	0.427840 (0.2%)
s820	1162	848	40 (3.44%)	38 (4.48%)	2	0.161060	0.147483 (8.43%)
s832	1293	948	84 (6.5%)	78 (12.04%)	5	0.239429	0.208798 (12.79%)
s953	415	312	88 (11.36%)	82 (26.28%)	6	0.369214	0.337811 (8.50%)

• Sharp upper bound in few regrowing steps

- $\bullet$  Improvement varies from 0.2% to 14%
- Uses a very low percentage of the size of the original graph
  - Lower than 10% (in most of cases)

### Performance Analysis (II): SMGs Regrowing Strategy (3) Experiments and Discussion (2)

Cranh	Si	ze	%	Size	Regrowing	Initial	Α
Graph	P	T	P'  (%)	T'  (%)	steps	thr. bound	0
s1423	1107	792	79 (7.13%)	76 (9.59%)	3	0.236010	0.235213 (0.34%)
s1488	1567	1128	91 (5.8%)	86 (7.62%)	6	0.201300	0.173127 (13.99%)
s208	27	24	27 (100%)	24 (100%)	3	0.409390	0.377683 (7.75%)
s27	54	44	19 (35.18%)	18 (40.9%)	1	0.305960	0.304987 (0.31%)
s349	187	146	26 (13.9%)	24 (16.44%)	2	0.340320	0.327867 (3.66%)
s444	92	68	14 (15.21%)	12 (17.64%)	2	0.181670	0.181260 (0.22%)
s510	1038	734	45 (4.33%)	40 (5.45%)	5	0.133030	0.117819 (11.43%)
s526	113	92	18 (15.93%)	16 (17.39%)	2	0.313490	0.305860 (2.43%)
s713	271	208	11 (4.06%)	10 (4.8%)	1	0.428720	0.427840 (0.2%)
s820	1162	848	40 (3.44%)	38 (4.48%)	2	0.161060	0.147483 (8.43%)
s832	1293	948	84 (6.5%)	78 (12.04%)	5	0.239429	0.208798 (12.79%)
s953	415	312	88 (11.36%)	82 (26.28%)	6	0.369214	0.337811 (8.50%)

• Sharp upper bound in few regrowing steps

- $\bullet\,$  Improvement varies from 0.2% to 14%
- Uses a very low percentage of the size of the original graph
  - Lower than 10% (in most of cases)

### Performance Analysis (II): SMGs Regrowing Strategy (3) Experiments and Discussion (3)

Graph	Original graph thr. CPU time (s)	Θ CPU time (s)	Original graph thr.	Θ	% thr.
s1423	59948.980	8.283	0.222720	0.235270	5.63%
s1488	36717.156	7.165	0.168760	0.172154	2.01%
s208	0.492	0.492	0.376892	0.376892	0%
s27	2166.002	0.954	0.305082	0.306166	0.35%
s349	141.210	0.441	0.328340	0.327398	-0.28%
s444	2278.231	0.205	0.181069	0.181260	0.11%
s510	13669.814	1.358	0.117500	0.118040	0.46%
s526	129.181	0.344	0.270010	0.305860	13.27%
s713	628.503	0.405	0.411630	0.427840	3.94%
s820	20775.811	0.788	0.144770	0.147699	2.02%
s832	16165.863	1.914	0.196920	0.208873	6.07%
s953	453.850	19.155	0.327910	0.338644	3.27%

• O CPU time insignificant respect to original thr CPU time

- Improvement varies from very close value to 13% over the real thr
  - Slow cycles far away from critical cycle?
- Negative relative error caused by simulation confidence interval

### Performance Analysis (II): SMGs Regrowing Strategy (3) Experiments and Discussion (3)

Graph	Original graph thr. CPU time (s)	Θ CPU time (s)	Original graph thr.	Θ	% thr.
s1423	59948.980	8.283	0.222720	0.235270	5.63%
s1488	36717.156	7.165	0.168760	0.172154	2.01%
s208	0.492	0.492	0.376892	0.376892	0%
s27	2166.002	0.954	0.305082	0.306166	0.35%
s349	141.210	0.441	0.328340	0.327398	-0.28%
s444	2278.231	0.205	0.181069	0.181260	0.11%
s510	13669.814	1.358	0.117500	0.118040	0.46%
s526	129.181	0.344	0.270010	0.305860	13.27%
s713	628.503	0.405	0.411630	0.427840	3.94%
s820	20775.811	0.788	0.144770	0.147699	2.02%
s832	16165.863	1.914	0.196920	0.208873	6.07%
s953	453.850	19.155	0.327910	0.338644	3.27%

- O CPU time insignificant respect to original thr CPU time
- Improvement varies from very close value to 13% over the real thr
  - Slow cycles far away from critical cycle?
- Negative relative error caused by simulation confidence interval

# Performance Analysis (III): PPNs Regrowing Strategy (1)

Which is the next p-semiflow constraining?

#### Generalising from SMGs to PPNs

- Previous method not longer valid
- Need other technique for next p-semiflow more likely to constrain

### Performance Analysis (III): PPNs Regrowing Strategy (1) Which is the next p-semiflow constraining?

### Generalising from SMGs to PPNs

- Previous method not longer valid
- Need other technique for next p-semiflow more likely to constrain

maximum 
$$\mathbf{y}' \cdot \mathbf{Pre} \cdot \mathbf{D}$$
  
subject to  $\mathbf{y}' \cdot \mathbf{C} = \mathbf{0}$   
 $\mathbf{y}' \cdot \mathbf{m}_{\mathbf{0}} = 1$   
 $\mathbf{y}'(p) \ge h, \ \forall p \in \mathbf{Q}$   
 $\sum_{p \in V} \mathbf{y}'(p) \ge h$   
where  $V = \{v | v \in \bullet(\|\mathbf{y}^*\|^{\bullet}) \setminus \|\mathbf{y}^*\|\}$   
 $Q = \{q \in P, q \in \|\mathbf{y}^*\|\}$ 

• Value *h* strictly positive and arbitrarily small

### Performance Analysis (III): PPNs Regrowing Strategy (1) Which is the next p-semiflow constraining?

### Generalising from SMGs to PPNs

- Previous method not longer valid
- Need other technique for next p-semiflow more likely to constrain

$$\begin{array}{l} \textit{maximum } \mathbf{y}' \cdot \mathbf{Pre} \cdot \mathbf{D} \\ \textit{subject to } \mathbf{y}' \cdot \mathbf{C} = \mathbf{0} \\ \mathbf{y}' \cdot \mathbf{m_0} = 1 \\ \mathbf{y}'(p) \geq h, \ \forall p \in \mathbf{Q} \\ \sum_{p \in V} \mathbf{y}'(p) \geq h \\ \textit{where } V = \{ v | v \in \bullet(\|\mathbf{y}^*\|^{\bullet}) \setminus \|\mathbf{y}^*\| \} \\ Q = \{ q \in P, q \in \|\mathbf{y}^*\| \} \end{array}$$

- Value *h* strictly positive and arbitrarily small
- Avoid numerical problems
   (h = 0) and LP feasible

maximum h

subject to  $\mathbf{y}\cdot\mathbf{C}=\mathbf{0}$ 

$$\mathbf{y} \cdot \mathbf{m_0} = 1$$

$$\mathbf{y} \geq h \cdot \mathbf{1}$$

h > 0

# Performance Analysis (III): PPNs Regrowing Strategy (2)

Algorithm 2 in the Dissertation

- Input data: PPN, accuracy
- Output data: sharp performance bound, bottleneck

# Performance Analysis (III): PPNs Regrowing Strategy (2)

Algorithm 2 in the Dissertation

- Input data: PPN, accuracy
- Output data: sharp performance bound, bottleneck

### Algorithm steps

- Calculate initial upper throughput bound and initial bottleneck cycle
- ② Calculate value h
- Iterate until no significant improvement is achieved or all places are considered
  - Compute the next constraining p-semiflow
  - ② Calculate new thr. bound

maximum  $\mathbf{y}' \cdot \mathbf{Pre} \cdot \mathbf{D}$ subject to  $\mathbf{y}' \cdot \mathbf{C} = \mathbf{0}$  $\mathbf{y}' \cdot \mathbf{m}_{\mathbf{0}} = 1$  $\mathbf{y}'(p) \ge h, \ \forall p \in \mathbf{Q}$  $\sum_{p \in V} \mathbf{y}'(p) \ge h$ where  $V = \{ v | v \in \bullet(\|\mathbf{y}^*\|^{\bullet}) \setminus \|\mathbf{y}^*\| \}$  $Q = \{ q \in P, q \in \|\mathbf{y}^*\| \}$ 

#### Motivation

4

#### Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling

#### Performance Analysis

- Some Background. . .
- Regrowing Strategy for SMGs
- Regrowing Strategy for PPNs

#### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

#### 6

#### **Resource Optimisation**

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
  - Problem Description
  - Performance Analysis
  - Resource Optimisation
- Conclusions

### Data-Throttling in Scientific Workflows (I) An intuitive idea: The slack concept



### Data-Throttling in Scientific Workflows (I) An intuitive idea: The slack concept



 $\delta$  execution time; tx = 1 transmission time

### Data-Throttling in Scientific Workflows (I) An intuitive idea: The slack concept



 $\delta$  execution time; tx = 1 transmission time

### Data-Throttling in Scientific Workflows (I) An intuitive idea: The slack concept



 $\delta$  execution time; t x = 1 transmission time

#### Assume tx = 1

- Slowest path:  $\Theta = \frac{1}{\sum(\delta + tx)} = \frac{1}{6}$ ( $\Theta$ : inverse of execution time of slowest path)
- Slack: how much faster is a path w.r.t. another until a synchronisation point

• 
$$\mu_{1,4} = \frac{2 - 1.5}{6} = \frac{0.5}{6}$$
  
•  $\mu_{4,6} = \frac{5 - 3.5}{6} = \frac{1.5}{6}$   
•  $\mu_{3,6} = \frac{5 - 3}{6} = \frac{1}{3}$ 

### Data-Throttling in Scientific Workflows (II) Automating Data-Throttling Analysis: An algorithm



- Inputs: Performance estimation (i.e., DAX annotations) + PN-based model
- Outputs: Data-throttling values + Analysis results

### Data-Throttling in Scientific Workflows (II) Automating Data-Throttling Analysis: An algorithm



- Inputs: Performance estimation (i.e., DAX annotations) + PN-based model
- Outputs: Data-throttling values + Analysis results
- 4 steps
  - Compute slack values
  - Oluster slacks
  - Compute data-throttling values
  - Performance analysis
    - With and w/out data-throttling

Data-Throttling in Scientific Workflows

Automating Data-Throttling Analysis

# Data-Throttling in Scientific Workflows (III)

Applying the algorithm to an example



#### Recall: slacks on synchronisation points

### Assumptions

- Bandwidth=100Mbps
- Data-sets equal to 10MiB
- Dedicated network topology
Automating Data-Throttling Analysis

# Data-Throttling in Scientific Workflows (III)

Applying the algorithm to an example



Recall: slacks on synchronisation points

### Assumptions

- Bandwidth=100Mbps
- Data-sets equal to 10MiB
- Dedicated network topology

- Slowest path:  $2 \rightarrow 5 \rightarrow 6$
- Slacks: μ<sub>1,4</sub>, μ<sub>3,6</sub>, μ<sub>4,6</sub>

Automating Data-Throttling Analysis

# Data-Throttling in Scientific Workflows (III)

Applying the algorithm to an example



### Recall: slacks on synchronisation points



Makespan: 5.6779 seconds

- Slowest path:  $2 \rightarrow 5 \rightarrow 6$
- Slacks: μ<sub>1,4</sub>, μ<sub>3,6</sub>, μ<sub>4,6</sub>

## Assumptions

- Bandwidth=100Mbps
- Data-sets equal to 10MiB
- Dedicated network topology

Automating Data-Throttling Analysis

# Data-Throttling in Scientific Workflows (III)

Applying the algorithm to an example



### Recall: slacks on synchronisation points



Makespan: 5.6779 seconds

# Assumptions

- Bandwidth=100Mbps
- Data-sets equal to 10MiB
- Dedicated network topology

- Slowest path:  $2 \rightarrow 5 \rightarrow 6$
- Slacks:  $\mu_{1,4}, \mu_{3,6}, \mu_{4,6}$ 
  - $1 \rightarrow 4$  adjust to 28.57%
  - $3 \rightarrow 6$  adjust to 35.15%
  - $4 \rightarrow 6$  adjust to 44.55%

Automating Data-Throttling Analysis

# Data-Throttling in Scientific Workflows (III)

Applying the algorithm to an example



# Assumptions

- Bandwidth=100Mbps
- Data-sets equal to 10MiB
- Dedicated network topology

### Recall: slacks on synchronisation points



- Slowest path:  $2 \rightarrow 5 \rightarrow 6$
- Slacks:  $\mu_{1,4}, \mu_{3,6}, \mu_{4,6}$ 
  - $1 \rightarrow 4$  adjust to 28.57%
  - $3 \rightarrow 6$  adjust to 35.15%
  - 4  $\rightarrow$  6 adjust to 44.55%

Data-Throttling in Scientific Workflows Experiments and Results

# Data-Throttling in Scientific Workflows (IV) Input Buffers Usage – some plots of Montage workflow tasks



 Data-throttling has great impact on input buffers • Outperforms both other topologies

R.J. Rodríguez

Ph.D. Dissertation

### Motivation

### Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling

### Performance Analysis

- Some Background. . .
- Regrowing Strategy for SMGs
- Regrowing Strategy for PPNs

### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

# 5

### Resource Optimisation

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
- Problem Description
- Performance Analysis
- Resource Optimisation
- Conclusions

Resource Optimisation

# Resource Optimisation (I)

### • Recall: FT systems with shared resources

• Can we add more resources to compensate throughput degradation?

Resource Optimisation

# Resource Optimisation (I)

# • Recall: FT systems with shared resources

- Can we add more resources to compensate throughput degradation?
- Yes, we can (some restrictions apply...)

Resource Optimisation

# Resource Optimisation (I)

# • Recall: FT systems with shared resources

• Can we add more resources to compensate throughput degradation?

• Yes, we can (some restrictions apply...)

### Considered approaches

- Budget limited while compensating a throughput degradation
- Budget unlimited while maintaining a given throughput

# Resource Optimisation (II): A heuristics

Algorithm 3 in the Dissertation - budget limited

- Input data: PPN, budget, resource costs
- Output data: Resource increments

# Resource Optimisation (II): A heuristics

Algorithm 3 in the Dissertation – budget limited

- Input data: PPN, budget, resource costs
- Output data: Resource increments

# Algorithm steps

- Initial bottleneck
- Iterate until no enough budget or next resource is process-idle place
  - Compute next constraining p-semiflow, and its associated resource (LPP in right column)
  - How much is this new increment?
- Solution When all resources are incremented and still enough budget → assign it

 $\begin{array}{l} \mbox{minimum } \sum_{j=1}^{k} \alpha_j \\ \mbox{subject to } \mathbf{y}_{k+1} \cdot \mathbf{Pre} \cdot \mathbf{D} = \mathbf{y}_1 \cdot \mathbf{Pre} \cdot \mathbf{D} \\ \mbox{y}_{k+1} \cdot \mathbf{C} = \mathbf{0} \\ \mbox{y}_{k+1} \cdot \mathbf{m}_{\mathbf{0}}^{\mathbf{\Delta}} = \mathbf{y}_j \cdot \mathbf{m}_{\mathbf{0}}^{\mathbf{\Delta}}, \ \forall j \in \{1 \dots k\} \\ \mbox{m}_{\mathbf{0}}^{\mathbf{\Delta}} = \left\{ \begin{array}{c} \mathbf{m}_{\mathbf{0}}(p) + \alpha_j, & p \in \mathbf{A} \\ \mathbf{m}_{\mathbf{0}}(p), & otherwise \\ \mbox{y}_{k+1}(p) = \mathbf{0}, \ p \in \mathbf{A} \\ \mbox{y}_{k+1}, \ \alpha_j \geq \mathbf{0}, \ \forall j \in \{1 \dots k\} \end{array} \right.$ 

# Resource Optimisation (III): Initial marking maintaining thr. Algorithm 4 in the dissertation – budget unlimited

- Input data: PPN with some FT added,  $\Theta,$  Set of p-semiflows added/modified when adding FTs
- Output data: Resource increments

# Resource Optimisation (III): Initial marking maintaining thr. Algorithm 4 in the dissertation – budget unlimited

- Input data: PPN with some FT added,  $\Theta,$  Set of p-semiflows added/modified when adding FTs
- Output data: Resource increments

# Algorithm steps

Iterate for each p-semiflow modified/added by the FT technique

 $\bullet\,$  Get maximum between current initial resource instances and the resources needed for maintaining giving  $\Theta\,$ 

# Resource Optimisation (IV): Guaranteeing minimum cost

$$\begin{array}{ll} \mbox{minimum} & \left(\sum_{i=1}^{n} c_{i}^{r} \cdot \alpha_{i} + \sum_{j=1}^{m} \left(c_{j}^{d} \cdot \beta_{j}^{d} + c_{j}^{c} \cdot \beta_{j}^{c} + c_{j}^{rm} \cdot \beta_{j}^{rm}\right)\right) \mbox{subject to} \\ \mbox{m}_{0}(r_{i}) + \alpha_{i} & \geq & \Theta \cdot \mathbf{y}_{i} \cdot \operatorname{Pre} \cdot \mathbf{D}' \\ \mbox{} \delta'(T_{detect}^{j}) & = & \delta(T_{detect}^{j}) - \beta_{j}^{d} \\ \mbox{} \delta'(T_{ee}^{j}) & = & \delta(T_{ee}^{j}) - \beta_{j}^{c} \\ \mbox{} \delta'(T_{ree}^{j}) & = & \delta(T_{ree}^{j}) - \beta_{j}^{rm} \\ \mbox{} \delta'(t) & \geq & \delta_{min}(t), \forall t \in T \\ \mbox{} \alpha_{i}, \beta_{j}^{d}, \beta_{j}^{c}, \beta_{j}^{rm} & \geq & 0, \alpha_{i} \in \mathbb{N}, \forall i \in [1 \dots n], \forall j \in [1 \dots m] \end{array} \right)$$

## Integer-Linear Programming Problem (ILPP)

• Minimum cost that guarantees a compensation of the throughput

# Resource Optimisation (IV): Guaranteeing minimum cost

$$\begin{array}{ll} \mbox{minimum} & \left( \sum_{i=1}^{n} c_{i}^{r} \cdot \alpha_{i} + \sum_{j=1}^{m} \left( c_{j}^{d} \cdot \beta_{j}^{d} + c_{j}^{c} \cdot \beta_{j}^{c} + c_{j}^{rm} \cdot \beta_{j}^{rm} \right) \right) \mbox{subject to} \\ \mbox{m}_{0}(r_{i}) + \alpha_{i} & \geq & \Theta \cdot \mathbf{y}_{i} \cdot \operatorname{Pre} \cdot \mathbf{D}' \\ \mbox{} \delta'(T_{detect}^{j}) & = & \delta(T_{detect}^{j}) - \beta_{j}^{d} \\ \mbox{} \delta'(T_{ec}^{j}) & = & \delta(T_{ec}^{j}) - \beta_{j}^{c} \\ \mbox{} \delta'(T_{rec}^{j}) & = & \delta(T_{rec}^{j}) - \beta_{j}^{rm} \\ \mbox{} \delta'(t) & \geq & \delta_{min}(t), \forall t \in T \\ \mbox{} \alpha_{i}, \beta_{i}^{d}, \beta_{i}^{c}, \beta_{i}^{rm} & \geq & 0, \alpha_{i} \in \mathbb{N}, \forall i \in [1 \dots n], \forall j \in [1 \dots m] \end{array}$$

## Integer-Linear Programming Problem (ILPP)

- Minimum cost that guarantees a compensation of the throughput
- Why an ILPP instead of a LPP?
  - Resource instances are natural numbers

### Motivation

### Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling

### Performance Analysis

- Some Background. . .
- Regrowing Strategy for SMGs
- Regrowing Strategy for PPNs

### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

### **Resource Optimisation**

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost



- Case Study: A Packet-Routing Algorithm
- Problem Description
- Performance Analysis
- Resource Optimisation

### Conclusions

Case Study: A Packet-Routing Algorithm Problem Description

# Case Study (I): Problem Description (1)



Case Study: A Packet-Routing Algorithm Problem Description

# Case Study (I): Problem Description (2)

A packet-routing algorithm: adding FT capabilities - reconfiguration with rollbackward



Case Study: A Packet-Routing Algorithm Performance Analysis

# Case Study (II): Performance Analysis (1)

A packet-routing algorithm with FT capabilities - reconfiguration with rollbackward

### • nP = 10, nT = 2 and nS = 2

# Case Study (II): Performance Analysis (1)

A packet-routing algorithm with FT capabilities - reconfiguration with rollbackward

- nP = 10, nT = 2 and nS = 2
- Reconfiguration with rollbackward
  - $\bullet~20\%$  of errors, and 5% of solid faults

# Case Study (II): Performance Analysis (1)

A packet-routing algorithm with FT capabilities - reconfiguration with rollbackward

- nP = 10, nT = 2 and nS = 2
- Reconfiguration with rollbackward
  - $\bullet~20\%$  of errors, and 5% of solid faults
- Before FT:  $\mathbf{y} = \{p_2, p_3, p_4, p_5, p_6|_{safe}, p_8|_{rtn}, p_9, p_{10}, p_{11}\}, \Theta = 0.470588$
- After FT:
  - New PN semiflows are known
  - $\mathbf{y}_1'$ ,  $\mathbf{y}_2'$  and  $\mathbf{y}_3'$ .  $\Theta_1=1.073825,\,\Theta_2=0.463768$  and  $\Theta_3=0.304762$
- New slowest:  $\Theta' = 0.304762 \rightarrow$  a degradation of 35.23%

Case Study: A Packet-Routing Algorithm Performance Analysis

# Case Study (II): Performance Analysis (2)

A packet-routing algorithm with FT capabilities: sensitive analysis



- $\Theta_1, \Theta_2$  and  $\Theta_3$  w.r.t.  $r_e, r_e \in [0 \dots 1]$
- $\Theta_2 < \Theta$  for low probabilities of error
  - Holds until  $r_e = 0.14$ . From that point,  $\Theta_3$  becomes slowest
  - Moreover, it exponentially decreases

# • $r_e \approx 0.8 ightarrow \Theta_1, \Theta_2$ and $\Theta_3$ quickly decrease and tend to zero

R.J. Rodríguez

Ph.D. Dissertation

June 24th, 2013

60 / 69

Case Study: A Packet-Routing Algorithm Resource Optimisation

# Case Study (III): Resource optimisation (1)

A packet-routing algorithm with FT capabilities: maintaining a given throughput

### • nP = 10, nT = 2 and nS = 2

# Case Study (III): Resource optimisation (1)

A packet-routing algorithm with FT capabilities: maintaining a given throughput

- nP = 10, nT = 2 and nS = 2
- Reconfiguration with rollbackward
  - $\bullet~20\%$  of errors, and 5% of solid faults

# Case Study (III): Resource optimisation (1)

A packet-routing algorithm with FT capabilities: maintaining a given throughput

- nP = 10, nT = 2 and nS = 2
- Reconfiguration with rollbackward
  - $\bullet~20\%$  of errors, and 5% of solid faults
- Before FT:  $\mathbf{y} = \{p_2, p_3, p_4, p_5, p_6|_{safe}, p_8|_{rtn}, p_9, p_{10}, p_{11}\}, \Theta = 0.470588$
- $\bullet$  Interest in maintaining  $\Theta$  while FT capabilities are present

# Case Study (III): Resource optimisation (1)

A packet-routing algorithm with FT capabilities: maintaining a given throughput

- nP = 10, nT = 2 and nS = 2
- Reconfiguration with rollbackward
  - $\bullet~20\%$  of errors, and 5% of solid faults
- Before FT:  $\mathbf{y} = \{p_2, p_3, p_4, p_5, p_6|_{safe}, p_8|_{rtn}, p_9, p_{10}, p_{11}\}, \Theta = 0.470588$
- $\bullet$  Interest in maintaining  $\Theta$  while FT capabilities are present
- $\mathbf{m}'_{\mathbf{0}}(p_0) = \mathbf{m}_{\mathbf{0}}(p_0) = 10, \mathbf{m}'_{\mathbf{0}}(p_2) = 3, \mathbf{m}'_{\mathbf{0}}(p_7) = 4$ 
  - Add another thread and two more filtering-threads to compensate a 20% of errors (and a 5% of them deriving in solid faults) using reconfiguration as FT technique

# Case Study (III): Resource optimisation (2)

A packet-routing algorithm with FT capabilities: maintaining a given throughput



• Initial resources to maintain  $\Theta = 0.470588, r_e \in [0...1]$ , steps of 0.01

# Case Study (III): Resource optimisation (2)

A packet-routing algorithm with FT capabilities: maintaining a given throughput



- Initial resources to maintain  $\Theta = 0.470588, r_e \in [0...1]$ , steps of 0.01
- No. packets and threads: remain equal
- No. filtering-threads: increases rapidly w.r.t.  $r_e$

R.J. Rodríguez

### Conclusions

### Motivation

### Security and FTTs Modelling

- Security Modelling
- Fault-Tolerant Techniques Modelling

### Performance Analysis

- Some Background. . .
- Regrowing Strategy for SMGs
- Regrowing Strategy for PPNs

### Data-Throttling in Scientific Workflows

- The Slack Concept
- Automating Data-Throttling Analysis
- Experiments and Results

### **Resource Optimisation**

- A heuristics
- Initial marking maintaining thr.
- Guaranteeing minimum cost
- Case Study: A Packet-Routing Algorithm
- Problem Description
- Performance Analysis
- Resource Optimisation

### Conclusions

- Security must be considered from the (early) beginning
- Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

- Security must be considered from the (early) beginning
- Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

Contributions of this Dissertation - a Summary

• SecAM: A UML Security Analysis and Modelling profile

- Security must be considered from the (early) beginning
- Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

- SecAM: A UML Security Analysis and Modelling profile
- $\bullet\,$  FTTs models (UML + PNs) helping to choose best suitable solution

- Security must be considered from the (early) beginning
- Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

- SecAM: A UML Security Analysis and Modelling profile
- FTTs models (UML + PNs) helping to choose best suitable solution
- Model-based methodology for performance prediction

- Security must be considered from the (early) beginning
- $\bullet\,$  Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

- SecAM: A UML Security Analysis and Modelling profile
- FTTs models (UML + PNs) helping to choose best suitable solution
- Model-based methodology for performance prediction
- Performance estimation based on upper thr. bounds computation

- Security must be considered from the (early) beginning
- $\bullet\,$  Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

- SecAM: A UML Security Analysis and Modelling profile
- FTTs models (UML + PNs) helping to choose best suitable solution
- Model-based methodology for performance prediction
- Performance estimation based on upper thr. bounds computation
- Data-throttling in scientific workflows: improvement of input buffer and network bandwidth usage

- Security must be considered from the (early) beginning
- Be careful with the impact of adding security  $\rightarrow$  trade-off analysis
- FT systems (sharing resources) modelled by PNs

- SecAM: A UML Security Analysis and Modelling profile
- FTTs models (UML + PNs) helping to choose best suitable solution
- Model-based methodology for performance prediction
- Performance estimation based on upper thr. bounds computation
- Data-throttling in scientific workflows: improvement of input buffer and network bandwidth usage
- Resource optimisation: increase no. resources while fulfilling requirements
# Conclusions (II)

### http://webdiis.unizar.es/GISED/?q=tool/peabrain



## Contribution: the PeabraiN tool

- PeabraiN: a tool for performance estimation and resource optimisation computation in Petri nets
  - GPL v3
  - JAVA-based

# Conclusions (II)

### http://webdiis.unizar.es/GISED/?q=tool/peabrain



## Contribution: the PeabraiN tool

- Peabrain: a tool for performance estimation and resource optimisation computation in Petri nets
  - GPL v3
  - JAVA-based

### Some stats

- 115 downloads (SF.net)
- Countries top three: Spain, France, Brazil

# Conclusions (III): Published Papers (1)

### Total numbers

- Two papers on JCR-indexed journals (SMC, JRR)
- Seven papers on international peer-review conferences (some CORE-indexed)

# Conclusions (III): Published Papers (1)

### Total numbers

- Two papers on JCR-indexed journals (SMC, JRR)
- Seven papers on international peer-review conferences (some CORE-indexed)
- Some more journals in progress. . .

# Conclusions (III): Published Papers (1)

### Total numbers

- Two papers on JCR-indexed journals (SMC, JRR)
- Seven papers on international peer-review conferences (some CORE-indexed)
- Some more journals in progress...

## Security and Fault-Tolerant Techniques Modelling

- Rodríguez, R. J., Trubiani, C., and Merseguer, J. Fault-Tolerant Techniques and Security Mechanisms for Model-based Performance Prediction of Critical Systems. In Proceedings of the 3rd International Symposium on Architecting Critical Systems (ISARCS), pages 21–30. ACM.
- Rodríguez, R. J., Merseguer, J. and Bernardi, S. Modelling and Analysing Resilience as a Security Issue within UML. In Proceedings of the 2nd International Workshop on Software Engineering for Resilient Systems (SERENE), ACM, 2010, 42–51.
- Rodríguez, R. J. and Merseguer, J. Giese, Integrating Fault-Tolerant Techniques into the Design of Critical Systems. In Proceedings of the 1st International Symposium on Architecting Critical Systems (ISARCS), Springer, 2010, 6150, 33–51.

# Conclusions (III): Published Papers (2)

### Performance Analysis and Resource Optimisation

- Rodríguez, R. J., Júlvez, J., and Merseguer, J. On the Performance Estimation and Resource Optimisation in Process Petri Nets. IEEE Transactions on Systems, Man, and Cybernetics: Systems, PP(99):1–14. doi: 10.1109/TSMC.2013.2245118
- Rodríguez, R. J., Júlvez, J., and Merseguer, J. Quantification and Compensation of the Impact of Faults in System Throughput. Proceedings of the Institution of Mechanical Engineers, Part O: Journal of Risk and Reliability. Accepted for publication.
- Rodríguez, R. J., Júlvez, J., and Merseguer, J. PeabraiN: A PIPE Extension for Performance Estimation and Resource Optimisation. In Proceedings of the 12th International Conference on Application of Concurrency to System Designs (ACSD), pages 142–147. IEEE.
- Rodríguez, R. J. and Júlvez, J. Accurate Performance Estimation for Stochastic Marked Graphs by Bottleneck Regrowing. In Proceedings of the 7th European Performance Engineering Workshop (EPEW), Springer, 2010, 6342, 175–190.

# Conclusions (III): Published Papers (2)

## Performance Analysis and Resource Optimisation

- Rodríguez, R. J., Júlvez, J., and Merseguer, J. On the Performance Estimation and Resource Optimisation in Process Petri Nets. IEEE Transactions on Systems, Man, and Cybernetics: Systems, PP(99):1–14. doi: 10.1109/TSMC.2013.2245118
- Rodríguez, R. J., Júlvez, J., and Merseguer, J. Quantification and Compensation of the Impact of Faults in System Throughput. Proceedings of the Institution of Mechanical Engineers, Part O: Journal of Risk and Reliability. Accepted for publication.
- Rodríguez, R. J., Júlvez, J., and Merseguer, J. PeabraiN: A PIPE Extension for Performance Estimation and Resource Optimisation. In Proceedings of the 12th International Conference on Application of Concurrency to System Designs (ACSD), pages 142–147. IEEE.
- Rodríguez, R. J. and Júlvez, J. Accurate Performance Estimation for Stochastic Marked Graphs by Bottleneck Regrowing. In Proceedings of the 7th European Performance Engineering Workshop (EPEW), Springer, 2010, 6342, 175–190.

### Performance Analysis Applied to Scientific Workflows

- Rodríguez, R. J., Tolosana-Calasanz, R., and Rana, O. F. Dynamic Data-Throttling in Scientific Workflows. To be submitted to IEEE Transactions in Parallel and Distributed Computing.
- Rodríguez, R. J., Tolosana-Calasanz, R., and Rana, O. F. Automating Data-Throttling Analysis for Data-Intensive Workflows. In Proceedings of the 12th IEEE/ACM International Symposium on Cluster, Cloud and Grid Computing (CCGrid), pages 310–317. IEEE.

Rodríguez, R. J., Tolosana-Calasanz, R. and Rana, O. F. Measuring the Effectiveness of Thottled Data Transfers on Data-Intensive Workflows. In Proceedings of the 6th International KES Conference on Agents and Multi-agent Systems – Technologies and Applications. Springer, 2012. 7327. 144–153.

## Acknowledgments

## Who support me (financially)

- Grupo de Investigación en Sistemas de Eventos Discretos
- DISC (INFSO-ICT-224498)
- DPI2006-15390, DPI2010-20413
- TIN2007-66523
- $\bullet\,$  DGA (CONAID) and CAI, ref. n. IT 5/11
- Ministry of Education, Culture and Sport, ref n. TME2011-00255

## Acknowledgments

## Who support me (financially)

- Grupo de Investigación en Sistemas de Eventos Discretos
- DISC (INFSO-ICT-224498)
- DPI2006-15390, DPI2010-20413
- TIN2007-66523
- $\bullet\,$  DGA (CONAID) and CAI, ref. n. IT 5/11
- Ministry of Education, Culture and Sport, ref n. TME2011-00255

### Who also support me (personally)

- Jorge & Merse
- DIIS staff
- Family, friends

• \*

Performance Analysis and Resource Optimisation of Critical Systems Modelled by Petri Nets

Ricardo J. Rodríguez

## Ph.D. DISSERTATION

Advisors: Dr. Jorge Emilio Júlvez Bueno and Dr. José Javier Merseguer Hernáiz



Dpto. de Informática e Ingeniería de Sistemas, Universidad de Zaragoza

June 24th, 2013

Zaragoza, Spain