Dealing with small data and training blind spots in the Manhattan world

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Abstract

Leveraging Manhattan assumption we generate metrically rectified novel views from a single image, even for non-box scenarios. Our novel views enable the already trained classifiers to handle training data missing views (blind spots) without additional training. We demonstrate this on end-to-end scene text spotting under perspective. Additionally, utilizing our fronto-parallel views, we discover unsupervised invariant mid-level patches given a few widely separated training examples (small data domain). These invariant patches outperform various baselines on small data image retrieval challenge.

1. Introduction

Discovering and matching patterns in images are two of the fundamental problems in computer vision. The key challenges are the pattern variations—scale, viewpoint, illumination or intra-class among others. Classical solutions involve matching features, such as SIFT [23], that are partially robust to some of these variations. These solutions encode local patterns in the image but do not attempt to correct for the viewpoint changes over the entire scene.

More recent methods (deformable part models [8], mid-level features [36] or deep neural networks [18]) have produced detectors with a higher degree of invariance by leveraging lots of training data to model the variation modes. These methods have shown to outperform those based on local descriptors in object and scene recognition tasks. But even in the current big data regime, handling these variations is still an open challenge [11]. This is specially true if the training data has blind spots or rarely occurring patterns [4, 45].

In addition, many scenarios, such as training models from one or few examples, have access to only small data. In this constrained data domain every possible 2D variation mode might not be present in the training set, and hence the approaches mentioned in the above paragraph have a poor performance. To put a few examples, imagine building a detector for every hotel using the few images on its website, for every apartment using its few sublet images, or for every lost luggage item using a few images from the trip album.

In this work we generate novel view-invariant representation to deal with the small data and the blind spots in the big data. In order to obtain such invariant representations we leverage the advances in single-image geometric scene understanding [15, 13, 14, 20, 43]. In a man-made scene, the entities are aligned mainly along three orthogonal directions (the Manhattan assumption); providing a cue about the observer’s orientation or viewpoint [29, 31]. Furthermore, the majority of the man-made scenes can be summarized into a stage model [15, 24] composed of a few dominant planes surrounding the viewing camera. The indoor scenes, for example, have a box-stage with 5 planes—floor, ceiling and left-center-right walls.

This stage model, along with the cues about the viewing camera parameters, allows us to reason in the 3D space instead of the 2D image pixel space and undo the projective transformation. Specifically, our algorithm uses such 3D cues to generate several metrically rectified novel views per image even for non-box Manhattan scenes. In each novel view, the entities aligned with its Manhattan direction are
Figure 2: Small data and blind spots. Discovering unsupervised invariant mid-level patches (g) from a few shots (small data), with little view variance (a) or matching-wise challenging wide separation (b) using our novel fronto-parallel views (c). Text spotter which missed the skewed text on the side walls (d), due to missing such training views (blind spots) (e), spots the same text (“SEX” and “PABLO”) using our novel views (f), with no extra training.

Contributions

1. Generation of metrically-rectified and world-aligned novel views from single image even for non-box Manhattan scenarios.

2. Unsupervised discovery of discriminative and 3D-invariant mid-level patches given limited training examples.

2. Related Work

Scene Based Reasoning. Much of the work on scene-level view-invariant representations focused on recovering the geometric layout of the scene from the image. In their pioneering work, Hoiem et al. [15] estimated the qualitative scene geometry from a single image. This 3D scene geometry lifted the reasoning from the 2D image space to the 3D physical world. Introducing physical rules helped to remove implausible detections in [16]. More recent works follow the similar goal of recovering 3D geometry by enforcing geometric and physical constraints [33, 37, 5, 34]. The work closest to ours is of Hedau et al. [14]. In addition to 3D physical reasoning, Hedau et al. generated affine rectified views to detect object cuboids. Differently from them, we generate metrically rectified plus aligned views. This world alignment enables us to correspond the content coming from different crowd-sourced images. Satkin et al. [31, 30] registered the 2D images within 3D CAD models using single image layout. This allowed to match wide-baseline views by registering them to the same CAD model. Our view invariance reasoning is entirely based on the image content, without requiring any meta-data like EXIF tags or scene CAD models. Savarese et al. [32] generate a subset of the unseen object views at test time by morph-
Scene Text Detection. The state-of-the-art scene text detectors have mainly focused on frontal text detection [40, 42, 1, 17] with special emphasis on cropped word detection [25]. Recently, Phan et al. [28] proposed cropped word detection on scene text under perspective. We extend the latest and show how image rectification improves end-to-end scene text spotting without additional training.

3. Generating Novel Views from Single Images

3.1. Manhattan Structure

In man-made scenes, entities are aligned mainly along three orthogonal directions (for example, the alignment of the room walls and the objects in Fig. 3a.) This is commonly known as the Manhattan assumption.

The Manhattan directions can be estimated by clustering the detected 2D line segments in an image into three dominant clusters (the red, green and blue line clusters in Fig. 3a). The intersection of the lines of each cluster gives the three vanishing points (VPs) [13, 29]. Each VP is associated with one of the Manhattan directions and constrains the scene structure. For example, the two axes of each plane segment are aligned with two of the VPs, e.g., the center wall in Fig. 3a is aligned with the red and green VPs. A line joining two VPs gives a scene horizon. For example, the horizontal horizon (magenta line in Fig. 3a) is defined by the green and blue VPs. The upward facing planes, e.g., floor, and the downward facing planes e.g., ceiling, cannot exist on the same side of the horizontal vanishing line. Therefore, the horizontal vanishing line forms a boundary between the top and the bottom parts of the scene (Fig. 3b). Similarly, the vertical horizon (yellow line in Fig. 3b) and the front horizon (black line in Fig 3b) divide the scene into left-right and front-back parts respectively. This gives us at most five parts (top, bottom, left, right, front). The number of scene parts changes with the location of the VPs. For example, if the blue VP exists outside the image on the left, there is no left part.

3.2. Aligned Fronto-Parallel Views

For every scene part from the previous section, our aim is to generate a metrically rectified view. In metric rectification, the aspect ratio of the 2D quadrilaterals remains constant [12]. For example, we want the checkers on the floor in Fig. 3a to be squares in the novel rectified images of the bottom part.

Viewing the same 3D plane from two calibrated views is constrained by the planar homography given in Eq. 1 [12]:

\[ H = K(R - \frac{tn^T}{d})K^{-1}, \]

where \( R \) and \( t \) are the relative rotation matrix and the translation vector between the two views and \( n \) and \( d \) are the
normal and distance to the origin of the plane. \(K\) stands for the internal calibration of the cameras, that we will take the same for the original and the novel views.

The image in Fig. 3a is taken from the magenta camera in Fig. 3c. In order to see the checkered pattern as squares, we want to place the camera facing the floor, i.e., the blue camera in Fig. 3c. Only a rotation is required to align the magenta and the blue camera. Setting \(t = 0\) in Eq. 1 gives

\[
H = KR_d^2R_i^2(\mathbf{K})^{-1},
\]

where \(R = R_d^2R_i^2; R_i^\phi\) standing for a rotation of a \(\phi\)-angle around the \(i\)-axis. The product \(KR_d^2\) is a similarity transform affecting the scale, in-plane rotation and the reflection that we will address later. The remaining part gives us the metric rectification in Eq. 3.

\[
H_m(\alpha, \beta) = R_d^2R_i^2(\mathbf{K})^{-1}
\]

Let \(\ell_i\) and \(\ell_j\) be the line segments forming the two axes of a checker. Their transformed counterparts using Eq. 3, i.e., \(H_m^{-1}\ell_i\) and \(H_m^{-1}\ell_j\), must be perpendicular to each other. Using this orthogonality constraint, the rotation angles, i.e., \(\alpha\) and \(\beta\) in Eq. 3, are estimated using the following minimization.

\[
\min_{\alpha, \beta} \sum_{i,j} |\ell_i^T \ell_j|,
\]

where \(\ell' = H_m^{-T}\ell\) and \(\hat{\ell}\) is the normal vector to \(\ell\). Note that the lines \(\ell_i\) and \(\ell_j\), are not the detected line segments from Fig. 3a. Unlike the approach taken by [43], we generate the line segments using the two VPs forming the horizon related to the current part. In Fig. 3b, the dashed lines (green and blue) are generated for the top part. This helps in rectifying the parts with little local line content, e.g., the ceiling in Fig. 3b. Finally, we calibrate the camera focal length \(f\) from the three VPs, using the code provided by [3, 9, 13]. If available, the EXIF data can also be used for camera calibration [43]. The optimization in Eq. 4 is repeated for all the scene parts.

So far, the homography in Eq. 3 only aligns the Z-axis of the novel camera view and the normal of its corresponding scene part (both shown as blue axis in Fig. 3c). This suffices to define the geometry of the problem up to a similarity transform; and approaches similar to the above have been used for single-view reconstruction (SVR) [22, 43]. As our aim is not SVR but obtaining invariant image representations, we still have to estimate the similarity transform (in-plane rotation and reflection) that aligns the image content of different images. Notice, for example, how the novel views of Fig. 3d are fronto-parallel but different (up to a similarity transform).

Our proposal for such alignment is as follows. We align the X and Y axes of the novel view with the X (horizontal) and the Y (vertical) axes of the corresponding scene part (X and Y axes correspond to red and green axes respectively in Fig. 3c). In other words, the X-axis is orthogonal to the vertical direction vector \((1\ 0)\) and Y-axis is orthogonal to the horizontal direction vector\((0\ 1)\). This transformation is given by Eq. 5:

\[
H_c(\gamma, \theta_1, \theta_2) = R_d^2R_y^\theta_1y^\gamma R_x^\theta_2x^\gamma,
\]

where \(\gamma\) is the in-plane rotation angle. \(\theta_1\) and \(\theta_2\) account for the mirror reflection, i.e., horizontal and vertical flipping (see first row in Fig. 3d for \(\gamma\) and \(\theta_2\)). At this point \(K\) only affects the digital zoom, so we drop it without loss of generality. These parameters are estimated using the following minimization:

\[
\arg\min_{\gamma, \theta_1, \theta_2} \left( \sum_i |\ell_i^{T'} [0, 1]| + \sum_j |\ell_j^{T'} [1, 0]| \right)
\]

\[
s.t. \gamma \in [0, 2\pi]; \theta_1, \theta_2 \in \{0, \pi\},
\]

where \(\ell'' = H_c^{-T}\ell\), \(\ell_i\) and \(\ell_j\) are the lines corresponding to the two VPs associated with the current scene part. The complete transformation is \(H_c = H_c^{-1}H_m\). Finally, the novel views for the top and the bottom part are rotated by \(0^\circ, 90^\circ, 180^\circ, 270^\circ\) to make them rotationally invariant. The bottom row in Fig. 3d, shows the 4 versions of the top view. These rotations are not required for the vertical parts (left, right and front) because in the crowd sourced data, the view variations in the vertical plane are \(<45^\circ\). Fig. 4 shows a few qualitative examples. For each view, the entities at only one orientation, irrespective of depth, are correctly rectified. This can be seen by comparing the green and yellow checkers (first Col. in Fig. 4) with the remaining multi-colored ones.

Before applying \(H_c\) to each scene part, we remove the area close to horizon lines (the gray area around horizons
in Fig. 3b). The points on the horizon lines are mapped to infinity by definition [12]. Additionally, the area near the horizon is magnified as compared to scene content away from horizon line. Therefore, in order to provide consistent levels of resolution, we subdivide each part into two sub-parts as shown as double arrows in Fig. 3a. Instead of using our rectification and applying random 3D rotations (using random parameters in Eq. 2) distorts the texture (Fig. 6). Using random 2D affine transformation provides some invariance (Fig. 6). However, as shown in the experimental section, these 2D transformations are not helpful.

4. Unsupervised Discovery Of Invariant Mid-Level Patches

After the geometry estimation of the previous section the scene can be divided into several parts, each one tentatively corresponding to a homography that rectifies that scene part to a canonical fronto-parallel view. We then generate a large collection of patches from these rectified views and we extract a number of “good” patches, i.e., patches that are discriminative to be used in classification and retrieval tasks. This approach is summarized in Algorithm 1, inspired by [36]. For the details read the referenced source.

Our goal is to recover these discriminative patches from a few widely separated views. For example in the two images (Fig. 5a, second row), it is difficult to match patches due to the high viewpoint variance. Our novel images (Fig. 5c) undo this variation. Therefore, we convert the training set (positive class \( P \) and negative world \( \mathcal{N} \)) into the rectified set \((P^r, N^r)\) using \( \text{H}_c = \text{H}_r \text{H}_m \). We perform the process (given in Algorithm 1) to recover the now invariant mid-level detectors.

Figure 5: Unsupervised discriminative patch discovery. [36] samples in the 2D image space, ours in the 3D space.

5. Implementation Details

For fronto-parallel views, the image is separated into five parts (left, right, top, bottom, front). Each part is subdivided into two parts. We use different versions of this subdivision for the patch discovery (solid double arrows in Fig. 3a) and the text detection (dashed double arrows in Fig. 3a). The bottom part is rotated at 0°, 90°, 180°, 270° for rotational invariance. We drop the top part, as its mostly non-informative. This gives at most 14 fronto-parallel views per image. For text spotting we only use the vertical views (left, right and center view) as the text existed mainly on the walls. For patch discovery, the minimum sampled patch size is 80x80 pixels and the maximum size is up to image size. The HoG feature, per patch, is 1984 dimensional, i.e., 8x8x31. A linear SVM is used with \( C = 0.1 \).

6. Datasets

6.1. The Hotels Dataset

Our first aim is to study the image retrieval task given a few training examples with high viewpoint difference. The existing available large datasets (Places [44], ImageNet [6]) do provide large viewpoint variance but with large intra-class variance. For example, in the bedroom class, the images mainly belong to different rooms. This is a more challenging problem. The NYU V2 dataset [35] has little intra-class variance. For example, in bedroom class, up to six images from the same bedroom are available but with little viewpoint variance. For our dataset we collected data of 68 different hotel interiors from http://www.
tripadvisor.com/. These images are uploaded by different visitors to these hotels. This provides large viewpoint variance. Additionally, the hotel interiors have little intra-class variance since they have repeating elements (e.g., bed type, bed sheets, carpets or curtains). Even with this specific style, image retrieval is difficult for the state of the art due to the specific attributes of this dataset, namely wide baseline viewpoints with little overlap and the small training size. We have 1360 training images (20 per hotel) and 680 test images (10 per hotel). Total 2040 images.

6.2. Places Dataset

For additional evaluation on a public dataset, we sampled ten categories from the Places dataset [44]. These categories include Art Gallery, Crosswalk, Kitchen, Laundromat, Locker room, Music studio, Pool room, Shoe Shop, Supermarket and Bathroom. We picked 10 train images and 10 test images per category (total 200 images) with low intra-class variation. Complementary to our Hotels dataset experiment, we manually removed the viewpoint overlap between the train and the test set. This makes the scenario even more challenging.

6.3. The Street View Text-Perspective (SVT-Perspective) Dataset [28]

SVT-Perspective [28] contains images of scenes with skewed text from Google Street View. It is composed of 238 images with 639 annotated words. Additionally, every image comes with a lexicon, i.e., names of nearby places (approx. 50) to reduce the search space at test time. The performance of the text detection baselines [40, 42] was noticeably degraded in this dataset compared with its fronto-parallel equivalent, the SVT (Street View Text) dataset [40]. Specifically, in our experiments, the F-scores of [40, 42] in the SVT dataset were respectively 0.380 and 0.460 and 0.100 and 0.114 in the SVT-Perspective one.

7. Experimental Results

7.1. Image Retrieval In Small Data Domain

7.1.1 Hotels Dataset

This section presents first a qualitative overview of the view-invariant discriminative patches extracted by our algorithm, followed by quantitative image retrieval results. Fig. 7 shows a comparison between the unsupervised mid-level patches of [36] (top row) and the view-independent ones using our algorithm (bottom row). The visual inspection of these patches reveals their complementary nature. Notice that mid-level view-specific patches include the spatial configuration of scene entities whereas our invariant model mainly captures distinctive planar patterns.

The invariance of the mid-level patches extracted by our algorithm can be further evaluated in Fig. 8. The first and the second row show the image patterns firing for a given mid-level detector and an invariant mid-level one respectively. Notice the view rigidity of mid-level detections (row 1) as compared to view agility of our patches (row 2). The different looking patterns in the second row look alike once rectified, as shown in row 3.

For quantitative analysis, in the first step, we selected a subset of our Hotels dataset (21 hotels, 15 training examples per hotel) for efficient discovery of top performing baselines, to be extensively evaluated later on. Table 1 shows a comparison of our algorithm and state-of-the-art
Table 1: Average image retrieval rates on our Hotels dataset (21 hotels, 15 train examples per hotel). BoW results are for the optimal dictionary size (200 words). * stands for rectified views only, †≤ 80 patches. This is the max number of patches detected for [36] on our dataset. ‡≤ 200 patches. Level refers to the spatial grid units (see section 7.1 for details).

<table>
<thead>
<tr>
<th>Method</th>
<th># Training Images</th>
<th>Ours</th>
<th>Ours+ + level 1</th>
<th>Ours+ + level 1 [36]</th>
<th>Ours+ + Mid-level [36]</th>
<th>Ours+ + level 2</th>
<th>Ours+ + level 2 [36]</th>
</tr>
</thead>
<tbody>
<tr>
<td>BoW [19]</td>
<td>80</td>
<td>0.26</td>
<td>0.21</td>
<td>0.21</td>
<td>0.21</td>
<td>0.21</td>
<td>0.21</td>
</tr>
<tr>
<td>Scene DPM [27]</td>
<td>80</td>
<td>0.36</td>
<td>0.37</td>
<td>0.37</td>
<td>0.37</td>
<td>0.37</td>
<td>0.37</td>
</tr>
<tr>
<td>GIST [26]</td>
<td>80</td>
<td>0.38</td>
<td>0.61</td>
<td>0.61</td>
<td>0.61</td>
<td>0.61</td>
<td>0.61</td>
</tr>
<tr>
<td>Mid-level† + level 1†</td>
<td>80</td>
<td>0.74</td>
<td>0.68</td>
<td>0.68</td>
<td>0.68</td>
<td>0.68</td>
<td>0.68</td>
</tr>
<tr>
<td>(Mid-level† [36] + 2D affine)† + level 1†</td>
<td>80</td>
<td>0.72</td>
<td>0.67</td>
<td>0.67</td>
<td>0.67</td>
<td>0.67</td>
<td>0.67</td>
</tr>
<tr>
<td>Ours‡ + level 1‡</td>
<td>80</td>
<td>0.83</td>
<td>0.77</td>
<td>0.77</td>
<td>0.77</td>
<td>0.77</td>
<td>0.77</td>
</tr>
<tr>
<td>Ours‡ + level 1‡</td>
<td>80</td>
<td>0.89</td>
<td>0.95</td>
<td>0.95</td>
<td>0.95</td>
<td>0.95</td>
<td>0.95</td>
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</table>

Table 1 shows several interesting conclusions. BoW in the original, non-rectified images performs better than its counterpart trained on our rectified ones. This shows that local features are not able to take advantage of our rectification. The results for scene DPM [27] are worse than those of a simpler global descriptor like GIST [26]. Scene DPM learns the 2D spatial configuration of the scene parts, a difficult task with limited training examples with large viewpoint variations.

Mid-level patches [36] perform better than CNN based deep features [44]. We used the pre-trained CNN (~2.5 million images) provided by the authors to extract a 4096-dimensional feature vector for one-versus-all SVM detection. Fine tuning the pre-trained net improved the performance but was still below the mid-level patches. Our Hotels dataset consists of repeating stylistic elements (carpet, bed sheets or bed type patterns). It is safe to conclude that, in this limited data domain, discriminative patches [36] capture better these mid-level elements than CNN [44].

Finally, our invariant detectors perform better than the mid-level viewpoint dependent detectors. For a fair comparison, we selected the same amount of patches, i.e., †≤ 80. These are the maximum patches discovered for [36] on our dataset. However, the performance of our method improves once we increase the number of patches, i.e., ‡≤ 200. Adding random 2D affine transformation to patches, helps in discovering more patches. However, they are not discriminative and they reduce the performance of standard mid level patches. The combination of mid-level patches and ours further improves the performance, indicating their complementary nature. For both methods, building a spatial pyramid over multiple grid levels does not help. The number of training parameters increases with the number of grid levels. Given the limited training set, this causes over-fitting. For level 1 we max-pooled over all scales to reduce the training parameters.

Next we further evaluate our approach for image retrieval on the entire Hotels dataset (68 classes) comparing the two top performers (ours, mid-level). The results (Fig. 9) are consistent with the results from the last section. Our approach consistently outperforms the mid-level baseline. The performance gap is wider in the small training data domain and as expected, decreases as we increase the training data. The combination of the two approaches outperforms the baselines showing their complementary nature. In our opinion, in the absence of entities with specific line/edge characteristics, the performance of this fusion reduces to the mid-level baseline. Adding Adaboost-based discriminative patch selection [38] performs slightly better (perspective view 9%, our novel views 10%) than BoW 8%, given 5 training examples. However, we achieve 51% and fusion with mid-level achieves 55%, given 5 training examples.
Figure 10: Text spotting under perspective distortion. The ground truth text is shown in a red box and the spotted text in a blue box. The top row shows the original images. The bottom row shows the novel view, generated by our proposal, where the text spotting algorithm [42] originally detected the text. (Last two columns) Text spotted which is even missed by the human annotators (“SUITES”, “HORNBLOWER”).

7.1.2 Places Dataset

Our view-invariant patches (72%) outperform mid-level patches (54%). As a small difference with the Hotels experiment, this time the fusion of both approaches shows little gain (73.4%) owing to little overlap between the train and the test sets. Additionally, the invariant patches discovered in this Places dataset (10 categories) represent objects, with little line/texture content (last row of Fig. 7), as opposed to the specific texture style (carpet, bed-sheet) in the Hotels dataset.

7.2. End-to-End Text Spotting under Perspective

In this section we show how our novel views help boosting the performance of already trained text spotters at test time and without additional training steps. The publicly available text spotters (pictorial-text detector [40], CNN-text detector [42]) have been trained on lots of real and synthetic data. However, they struggle to cope with the perspective distortion. Table 2 shows their F-scores.

The major feature in the pictorial spotter [40] is the spacing between the detected individual characters. This spacing must be close to one character size. Under perspective distortion (some examples in Fig. 10, top row) the relative size of the characters and their spacing gets distorted, confusing the detector. Our novel views restore the scale and the spacing consistency (Fig. 10, bottom row).

The convolutional spotter [42] segments in a first step the horizontal lines of foreground text in the image. These text lines are detected at multiple scales. However, at a single scale the characters must have similar size, resulting in rectangular boxes. Under perspective distortion the characters closer to the viewer appear at a different scale compared to the far field characters (Fig. 10, top row). Furthermore, the spacing between the characters decides the segmentation of the foreground text line into multiple text boxes. A distorted spacing might lead to an incorrect segmentation that degrades the performance. Our novel views restore this scale and character spaces and convert oblique perspective lines into horizontal ones, leading to better performance. Even the deep text spotters [17] are affected by the perspective distortion [41]. Differently to [41], our novel views aid in the detection step rather than the subsequent classification step. Additionally note that the text spotting examples are not entirely box-like (Fig. 10, first column). Our novel views work even in outdoor quasi-Manhattan scenarios.

Table 2: Text Detection F-scores (SVT-Perspective dataset)

<table>
<thead>
<tr>
<th></th>
<th>Baseline</th>
<th>Baseline + Ours</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wang [40]</td>
<td>0.100</td>
<td>0.144</td>
<td>0.179</td>
</tr>
<tr>
<td>Wang-Wu [42]</td>
<td>0.114</td>
<td>0.144 + Ours</td>
<td>0.207</td>
</tr>
</tbody>
</table>

8. Conclusion and Future Work

Our novel view-invariant representation enables pattern discovery given small data (as shown in the image retrieval task). It also enables the already trained detectors to cater for the training data blind spots (as shown in the text spotting task). Our 3D invariant mid-level detectors are a small step towards unsupervised 3D scene understanding with small data. In a recent related approach [10], fusing such invariant mid-level patches with big data has enabled unsupervised single view surface orientation estimation. Future work involves discovering 3D relations amongst our unsupervised patches. Such relations might lead to exciting algorithms like unsupervised 3D DPM.

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